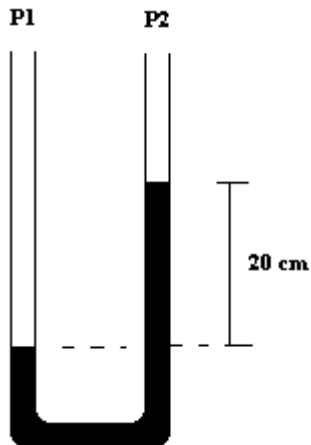


TOPIC

Fluids – Section X – Question 3

QUESTION

Consider the manometer shown. The dark fluid is mercury (density = 13.6 gm/cm^3) and the light fluid is water (density = 1 gm/cm^3). The difference in pressure $P_1 - P_2$ in kPa most nearly is

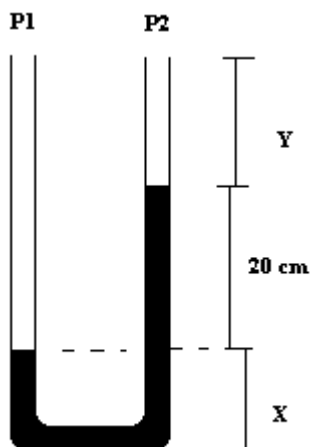


- (A) 2.00
- (B) 22.7
- (C) 24.7
- (D) 26.7

HINTS

- Pressure in a fluid depends on height of fluid by ρgh where h is the height of fluid.
- The pressure at the bottom of the tube is the same whether calculated from the left or the right branch.

SOLUTION



Let the pressure at the bottom of the tube $=P_0$. Then P_0 is related to P_1 by

$$P_0 = P_1 + \rho_{\text{water}}g(Y + 20) + \rho_{\text{mercury}}gX$$

and is related to P_2 by

$$P_0 = P_2 + \rho_{\text{water}}g(Y) + \rho_{\text{mercury}}g(X + 20)$$

Equating the two expressions yields:

$$\begin{aligned} P_1 - P_2 &= 20g(\rho_{\text{mercury}} - \rho_{\text{water}}) \\ &= (20\text{cm})(980\text{cm/s}^2)(13.6\text{gm/cm}^3 - 1\text{gm/cm}^3) \\ &= (20\text{cm})(980\text{cm/s}^2)(12.6\text{gm/cm}^3) \\ &= 247,000\text{gm/cm-s}^2 \times 1\text{kg}/1000\text{ gm} \times 100\text{cm}/1\text{m} \\ &= 24,700\text{kg/m-s}^2 \\ &= 24,700\text{Pa} \\ &= 24.7\text{kPa} \end{aligned}$$

ANSWER

(C)

CONTRIBUTOR

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