TOPIC

Mathematics – Section I – Question 3

QUESTION

The Newton-Raphson method formula for finding the square root of a real number R from the equation $x^2 = R$ is

$$(A) x_{i+1} = \frac{x_i}{2}$$

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(B) $x_{i+1} = \frac{3x_i}{2}$

(C)
$$x_{i+1} = \frac{1}{2} \left(x_i + \frac{R}{x_i} \right)$$

(D)
$$x_{i+1} = \frac{1}{2} \left(3x_i - \frac{R}{x_i} \right)$$

HINT

Rewrite the equation in the form f(x) = 0, that is,

$$f(x) = x^2 - R = 0$$

Now apply the Newton's formula

$$x_{i+1} = x_i - \frac{f(x_i)}{f'(x_i)}$$

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