

TOPIC

Engineering Mechanics (Statics and Dynamics) – Section VII – Question 9

QUESTION

A body is traveling in a straight line. The equation of motion is given by

$$x(t) = 5t^3 + 3t^2 - 6t$$

where

 x is given in meters, and t is given in seconds.The acceleration of the body in m/s^2 at $t = 5.25$ seconds most nearly is

(A) 6.000

(B) 163.5

(C) 436.8

(D) 752.9

HINT

Acceleration = $\frac{d^2x}{dt^2}$. So differentiate the expression of location x , twice with respect to time to get the expression for acceleration.

SOLUTION

The velocity

$$\begin{aligned}v &= \frac{dx}{dt} \\&= \frac{d}{dt}(5t^3 + 3t^2 - 6t) \\&= 15t^2 + 6t - 6\end{aligned}$$

The acceleration is given by

$$\begin{aligned}a &= \frac{dv}{dt} \\&= \frac{d}{dt}(15t^2 + 6t - 6) \\&= 30t + 6 \\&= 30 \times 5.25 + 6 \\&= 163.5 \text{m/s}^2\end{aligned}$$

ANSWER

(B)

CONTRIBUTOR

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